GYAN BHARATI SCHOOL

Pre Board Examination (2023-24)

Mathematics (041)

Class - SS2

Set A



Time: 3 Hrs.

Marks: 80

General Instructions:

- 1. There are five printed pages in this question paper.
- 2. This Question paper contains five sections A, B, C, D and E. Each section is compulsory. However, there are internal choices in some questions.
- 3. Section A has 18 MCQ's and 02 Assertion-Reason based questions of 1 mark each.
- 4. Section B has 5 Very Short Answer (VSA)-type questions of 2 marks each.
- 5. Section C has 6 Short Answer (SA)-type questions of 3 marks each.
- 6. Section D has 4 Long Answer (LA)-type questions of 5 marks each.
- 7. Section E has 3 source based/case based/passage based/integrated units of assessment of 4 marks each with sub-parts.

Section - A

Q1 The Cartesian equation of a line is given by
$$\frac{2x-6}{3} = \frac{3y-7}{2} = \frac{4z-7}{-2}$$
. Its direction ratios are (1)

- (a) 3,2,-2
- (b) 9,-4,3
- (c) 9,4,-3
- (d) 3,-2,2

Q2 Value of
$$\int_0^1 \frac{dx}{9-4x^2}$$
 is (-)

- $(a) \frac{1}{2} ln5$
- (b) $-\frac{1}{12}ln5$
- (c) $\frac{1}{3}ln5$
- (d) $\frac{1}{12} ln5$

Q3

If
$$A = \begin{pmatrix} 1 & 1 & 1 \\ 2 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
, then value of $A^2 - 2A$ is

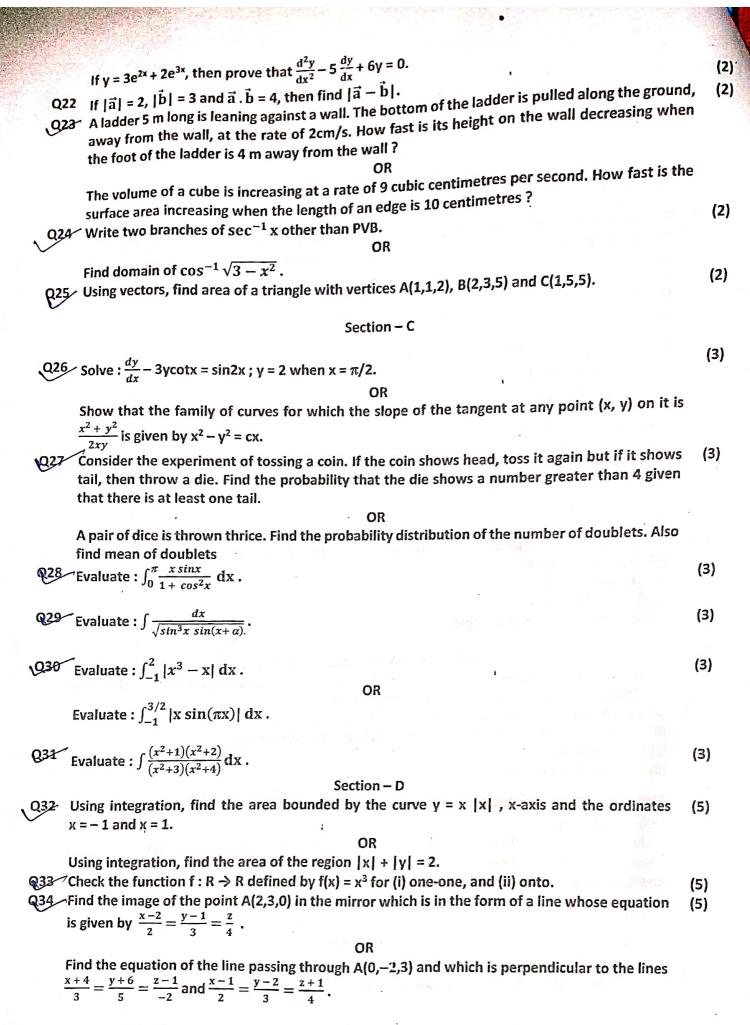
- (a) $\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 0 & -1 \end{pmatrix}$
- (b) $\begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 1 \end{pmatrix}$
- (c) $\begin{pmatrix} 1 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$
- (d) $\begin{pmatrix} 1 & 0 & 0 \\ 2 & 1 & 2 \\ 1 & 3 & 0 \end{pmatrix}$

- (b) < 1,0,0 >, < 0,1,0 >, < 0,0,1 >
- (c) <-1.0.0>, <0.-1.0>, <0.0.1>
- (d) < 1,0,0 >, < 0,1,0 >, < 0,0,-1 >

(1)

```
Q5
          Value of 'k' so that f(x) = \begin{cases} \frac{x}{|x| + 2x^2} & \text{when } x \neq 0 \\ k & \text{when } x = 0 \end{cases} may be continuous at x = 0, is
                                                                                                                                               (1)
          (a) 2
          (b) -2
          (c) does not exist
          (d) can't be decided
         Value of sec^{-1} sec\left(-\frac{11\pi}{3}\right) is
 Q6
                                                                                                                                                (1)
          (a) 2\pi/3
         (b) -\pi/3
         (c) \pi/2
         (d) \pi/3
         Let A(1,2), B(2,1), C(3,4) and D(3,2) be feasible points of a bounded region and we need to
 Q7
                                                                                                                                                (1)
         maximize z = -x + y. Maximum value occurs at (chose best possible answer):
         (a) A(1,2)
         (b) C(3,4)
         (c) all points on the line segment AC
         (d) A and C only
         If A and B are independent events, then A' and B' are
                                                                                                                                               (1)
         (a) independent events
         (b) not necessarily independent events
         (c) can't be decided
         (d) none of these
Q9
         Derivative of 2\sqrt{\cot x^2} w.r.t. 'x' at x = \sqrt{\frac{\pi}{4}} is
                                                                                                                                               (1)
         (a) -\sqrt{\pi}
         (b) -2\sqrt{\pi}
         (c) 2\sqrt{\pi}
         (d) \sqrt{\pi}
Q10
         If \begin{bmatrix} a-b & 2a+c \\ 2a-b & 3c+d \end{bmatrix} = \begin{bmatrix} -1 & 5 \\ 0 & 13 \end{bmatrix}, then a+b+c+d is
                                                                                                                                              (1)
         (b) 9
         (c) 10
         (d) 1.1
Q11 If |\vec{a}| = |\vec{b}|, then \vec{a} and \vec{b} are
                                                                                                                                              (1)
         (a) equal vectors
         (b) different vectors
        (c) can't be decided
        (d) not necessarily equal vectors
Q12 If x^3 + xy^2 + x^2y + y^3 = 10, then dy/dx is
                                                                                                                                              (1)
        (a) \frac{3x^2 + 2xy + y^2}{x^2 + 2xy + 3y^2}
       If \begin{vmatrix} x & 2 \\ 18 & x \end{vmatrix} = \begin{vmatrix} 6 & 2 \\ 18 & 6 \end{vmatrix}, then x is
                                                                                                                                              (1)
        (a) 6
        (b) -6
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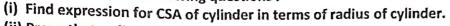
 $(c) \pm 6$ (d) 0 Q14 (1) Unit vector in the direction of sum of the vectors $2\hat{\imath} - 2\hat{\jmath} + 3\hat{k}$ and $3\hat{\imath} - 6\hat{\jmath} + \hat{k}$ is (b) $\frac{2\hat{i}-6\hat{j}+4\hat{k}}{\sqrt{56}}$ (c) $\frac{5\hat{1}-8\hat{j}-4\hat{k}}{\sqrt{105}}$ (d) $\frac{5\hat{1}+8\hat{j}-4\hat{k}}{\sqrt{105}}$ Q15 Assume X, Y, Z, W and P are matrices of order $2 \times n$, $3 \times k$, $2 \times p$, $n \times 3$ and $p \times k$, respectively. (1) The restriction on n, k and p so that PY + WY will be defined are (a) k = 3, n = 3(b) k is arbitrary, p = 2(c) p is arbitrary, k = 3(d) k = 2, p = 3(1) Q16 Solution of $\frac{dy}{dx} = \frac{x+1}{2-y}$; $y \neq 2$, is (a) $2x^2 + y^2 + x - 4y = c$ (b) $x^2 + 2y^2 + 2x - y = c$ (c) $x^2 + y^2 + 2x - 4y = c$ (d) $2x^2 + 2y^2 + x - 3y = c$ (1) Q17 If A is an invertible matrix of order 4 and |adjA| = 125, then |A| is (a) 25 (b) ± 25 (c) 125 (d) 5 (1) Q18 The points A(2î – ĵ + k̂), B(î – 3ĵ – 5k̂) and C(3î – 4ĵ – 4k̂) are the vertices of (a) equilateral triangle (b) isosceles triangle (c) right angled triangle (d) right angled isosceles triangle ASSERTION-REASON BASED QUESTIONS In the following 2 questions, a statement of Assertion (A) is followed by a statement of Reason (R). Choose the correct answer out of the following choices: (a) Both A and R are true and R is the correct explanation of A. (b) Both A and R are true but R is not the correct explanation of A. (c) A is true but R is false. (d) A is false but R is true. Assertion : Order and degree of differential equation $2x \left(\frac{d^2y}{dx^2}\right)^2 + \cos\left(\frac{dy}{dx}\right) = 0$ are 2 and not Q19 defined, respectively. Reason: Order of a differential equation is highest derivative present and degree is highest power of derivatives present. (1) Assertion: $x^2 e^{-x}$ is strictly increasing in the interval (0, 2). Reason: f(x) is strictly increasing in an interval if f'(x) > 0. Section - B 921 If $x = a(\cos t + \log(\tan \frac{t}{2}))$, $y = a \sin t$, then find $\frac{dy}{dx}$ in simplified form. (2)



O35 The sum of three numbers is 6. If we multiply third number by 3 and add second number to it, we get 11 Represent (5) we get 11. By adding first and third numbers, we get double of the second number. Represent it algebraically and find the numbers using matrix method.

Section - E

- Q36 Cost function for running a business is given by C = 50x + 20y where x and y are variables subject to following constraints: $2x - y \ge -5$; $3x + y \ge 3$, $2x - 3y \le 12$, $x \ge 0$; $y \ge 0$ Based on above information, answer following questions, graphically:
 - (i) Find all feasible points which can contribute to minimum cost. (2)
 - (ii) Find minimum cost. (2)
- Q37 A company is making toys in the shape of a right circular cone in which a right circular cylinder having maximum curved surface area, is inscribed. Take radius and height of cone as r and h respectively. Based on the above information, answer following questions:



- (ii) Prove that radius of cylinder is half of the radius of the cone.
- (iii) Find the maximum CSA of cylinder.



(2) (1)

(2)

(1)

- Q38 Two groups are competing for the position in Board of directors of a corporation. They both want to introduce a new product for increasing profit of company. The probabilities that the first and the second groups will win are 0.6 and 0.4 respectively. Further, if the first group wins, the probability of introducing a new product is 0.7 and the corresponding probability is 0.3 if the second group wins. Based on above information, answer following questions:
 - (i) What is the probability that the new product is introduced?
 - (2) (ii) Find the probability that the new product introduced was by the second group.

OR

(ii) Find the probability that the new product introduced was by the first group.