

Shubham
x8

CAMBRIDGE SCHOOL, SRINIWASPURI

Class: XI
Time : 3 Hrs.

HALF YEARLY EXAMINATION - 2015

M.M. 100
Sub: maths

General instructions:

All questions are compulsory

Q.1 to Q.6 carries one mark each.

Q.7 to Q.19 carries four marks each

Q.20 & Q.26 carries six marks each

1. If $(x+1, y-2) = (3, 1)$ then find x & y .

2. If $f(x) = x^2 + 7$ & $g(x) = 3x - 15$ then find $f(3) + g(-5)$.

3. Evaluate: $(1+i)^6 + (1-i)^6$.

4. Find the modulus of $12i + 5$.

5. Find the H.C.F. of $4!$; $5!$; & $6!$.

6. Find the 13th term in $(9x - \frac{1}{3\sqrt{x}})^{18}$; x not equal to zero.

7. Two finite sets have 'm' & 'n' elements. If the total number of subsets of 1^{st} is 56 more than the total number of subsets of the 2^{nd} find 'm' & 'n'.

8. Prove using Venn-Diagram: $A \cap (A^c \cup B) = A \cap B$. OR $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$.

9. Find the domain & range of $f(x) = \sqrt{x-1}$

OR

Define $R = \{(x, y) : y = x + 5; x \text{ is a natural number less than } 5\}$ depict R in roster form & find its domain & range.

10. If $P = \{5, 6\}$ & $Q = \{3, 7, 8\}$, then find $P \times Q$; $Q \times P$; $P \times P \times P$.

11. Find the conjugate of $\frac{(3-2i)(3i+2)}{(1+2i)(2-i)}$.

12. Solve: $2x^2 + ix\sqrt{15} - 1 = 0$.

13. Suppose most of your clothes are dirty & you are left with 2 pants & 3 shirts. How many choices do you have?

OR

There are 6 flavours of ice cream, & 3 different cones. How many different single scoop ice creams can you order?

14. Find n when $P(n-1,3) : P(n,4) = 1 : 9$.

15. Solve & represent the solution on the number line : $5(2x-7) - 3(2x+3) \leq 0$ & $2x+9 \leq 6x+47$.

OR

$$\frac{3x-7}{2} \geq \frac{x+1}{4} \quad \& \quad 2x+9 \geq 6x+7$$

16.(a) Express $\sin 4x - \sin 2x$ as a product of trigonometric functions.

(b) Prove : $\frac{\sin(x+y)}{\sin(x-y)} = \frac{\tan x + \tan y}{\tan x - \tan y}$.

17. Prove : $\frac{\sec 8x - 1}{\sec 4x - 1} = \frac{\tan 8x}{\tan 2x}$.

18. Show that $\cot x \cot 2x - \cot 2x \cot 3x - \cot 3x \cot x = 1$.

19. Find the term independent of x in $\left(\frac{3x^2}{2} - \frac{1}{3x}\right)^6$

20. Solve graphically : $x - 2y \leq 3$; $3x + 4y \geq 12$; $x \geq 0$; $y \geq 1$.

21. If the coefficients of 3 consecutive terms in the expansion of $(1+a)^n$ are in the ratio of 1 : 7 : 42. Find 'n'.

OR

The 2nd, 3rd & 4th terms in the binomial expansion of $(x+a)^n$ are 240, 720, & 1080. Find x , a , & n .

22. Solve : (i) $\cot^2 x + \operatorname{cosec} x + 3 = 0$; (ii) $\cos x + \cos 3x + \cos 5x + \cos 7x = 0$.

23. If $\operatorname{cosec} x = -13/12$ & x lies in the 3rd quadrant. Then find $\tan x$, $\sec x$ & $\cos x$. Also find $\tan 75^\circ$.

24.(i) How many chords can be drawn through 21 points on a circle.

(ii) If there are 20 persons in a party & if each of them shakes hand with one another, how many handshakes happen in the party.

25. In an examination, a paper consists of 12 questions divided into 2 parts each containing 5 & 7 respectively. A student is required to attempt 8 questions in all, selecting at least 3 from each part. In how many ways can a student select the questions?

26. In a group of 50 persons, 14 drink fruit juice but not cold drink; 30 drink fruit juice & each person likes at least one of the 2 drinks. Find (a) how many drink both. (b) drink cold drink but not fruit juice.

OR

If $A = \{3,5,7,9,11\}$; $B = \{7,9,11,13\}$; $C = \{11,13,15\}$; $D = \{15,17\}$ find (i) $A-B$ (ii) $A \cap C$ (iii) $C \cup D$ (iv) $A \cap B \cup D$.

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