

17

XI-D

N.K. BAGRODIA PUBLIC SCHOOL, DWARKA
FIRST TERM EXAMINATION (2017-18)
CLASS - XI
MATHS

Minika Dobhal

M.M. : 100

TIME : 3 Hrs.

GENERAL INSTRUCTIONS :

1. This question paper has 4 pages
2. All questions are compulsory.
3. Section A has Q. 1-4 which carries 1 mark each.
Section B has Q. 5-12 which carries 2 marks each.
Section C has Q. 13-23 which carries 4 marks each.
Section D has Q. 24-29 which carries 6 marks each.
4. Use of calculator is not allowed.

SECTION A

Q1 Find the value of $8\cos^3 \frac{\pi}{9} - 6\cos \frac{\pi}{9}$

Q2 If 'n' is any integer, then find the value of $(1 - i)^n \left(1 - \frac{1}{i}\right)^n$

Q3 Find $(n+1)^{\text{th}}$ term from the end in the expansion of $\left(x - \frac{1}{x}\right)^{3n}$

Q4 If $A = 1 + r^a + r^{2a} + \dots + \infty$ and
 $B = 1 + r^b + r^{2b} + \dots + \infty$ then find $r^a \cdot r^b$

SECTION B

Q5 Find real ' θ ' such that $\frac{3 + 2i\sin\theta}{1 - 2i\sin\theta}$ is purely real. ✓

Q6 If a, b, c are in A.P. ; b, c, d are in G.P. and $\frac{1}{c}, \frac{1}{d}, \frac{1}{e}$ are in A.P. prove that a, c, e are in G.P.

Q7 Find the sum of 'n' terms of series : $\frac{1}{1 \times 2} + \frac{1}{2 \times 3} + \frac{1}{3 \times 4} + \dots$

Q8 ✓ If x^p occurs in the expansion of $\left(x^2 + \frac{1}{x}\right)^{2n}$

Prove that its coefficient is $\frac{(2n)!}{\left(\frac{4n-p}{3}\right)! \left(\frac{2n+p}{3}\right)!}$

Q9 ✓ In any ΔABC , prove that :
 $a \sin(B-C) + b \sin(C-A) + c \sin(A-B) = 0$

Q10 Solve the following system of inequalities :
 $|x-1| \leq 5, |x| \geq 2$

Q11 ✓ Find the $\sin \frac{x}{2}, \cos \frac{x}{2}$ if $\sin x = \frac{1}{4}$, where x lies in second quadrant.

Q12 In how many ways 5 boys and 3 girls be seated in a row so that no two girls are together ?

SECTION C

Q13 ✓ By using principle of Mathematical Induction, prove that $2 \cdot 7^n + 3 \cdot 5^n - 5$ is divisible by 24 for all $n \in \mathbb{N}$.

Q14 Solve the system of linear inequalities graphically :
 $x + 2y \geq 0, 2x + y \leq 4, x > 0, y < 2$

Q15 ✓ If the A.M. and G.M. between two numbers are in the ratio $m : n$, then prove that the numbers are in the ratio $m + \sqrt{m^2 - n^2} : m - \sqrt{m^2 - n^2}$

Q16 ✓ Convert the following complex number into polar form :

$$\frac{i-1}{\cos \frac{\pi}{3} + i \sin \frac{\pi}{3}}$$

Q17 ✓ In any ΔABC , prove that :
 $(b^2 - c^2) \cot A + (c^2 - a^2) \cot B + (a^2 - b^2) \cot C = 0$

Q18 ✓ If α and β are different complex number with $|\beta| = 1$, then find $\left| \frac{\beta - \alpha}{1 - \bar{\alpha}\beta} \right|$

Q19 Solve the following equations :

$$4 \sin x \cos x + 2 \sin x + 2 \cos x + 1 = 0$$

OR

$$\sin x \tan x - 1 = \tan x - \sin x$$

Q20 How many words with or without meaning, each of 2 vowels and 3 consonants can be formed from the letters of the word 'HONESTY' ?

Write the importance of HONESTY in our life.

Q21 Find the coefficient of x^4 in the expansion of the product $(1 + 2x)^4 (2 - x)^5$

OR

Find the value of 'K' so that the term independent of 'x' in the expansion of $\left(\sqrt{x} - \frac{K}{x^2}\right)^{10}$ is 405.

Q22 If the coefficients of three consecutive terms in the expansion of $(1+x)^n$ are in the ratio 1 : 7 : 42, find n.

Q23 The difference between any two consecutive interior angles of a polygon is 5° . If the smallest angle is 120° , find the number of sides of polygon.

OR

If 'a', 'b' are the roots of $x^2 - 3x + p = 0$ and c, d are the roots of $x^2 - 12x + q = 0$.

Where a, b, c, d form a G.P., prove that :

$$(q + p) : (q - p) = 17 : 15$$

SECTION D

Q24 If a_1, a_2, a_3 and a_4 are coefficients of any four consecutive terms in the expansion of $(1+x)^n$, prove that : $\frac{a_1}{a_2 + a_1} + \frac{a_3}{a_3 + a_4} = \frac{2a_2}{a_2 + a_3}$

Q25 Prove that :

$$\sin 10^\circ \sin 30^\circ \sin 50^\circ \sin 70^\circ = \frac{1}{16}$$

OR

a) Prove that :

4

$$\cos^2 x + \cos^2 \left(x + \frac{\pi}{3} \right) + \cos^2 \left(x - \frac{\pi}{3} \right) = \frac{3}{2}$$

b) Prove that : $\frac{\sec 8x - 1}{\sec 4x - 1} = \frac{\tan 8x}{\tan 2x}$

2

Q26 a) Find the sum to 'n' term of series :

4

$$5 + 7 + 13 + 31 + 85 + \dots$$

b). If a, b, c are in G.P. and $a^{1/x} = b^{1/y} = c^{1/z}$ then prove that x, y, z are in A.P.

2

Q27 a) Find the square root of 1-i

4

b). If $x - iy = \sqrt{\frac{a - ib}{c - id}}$ then prove that : $(x^2 + y^2)^2 = \frac{a^2 + b^2}{c^2 + d^2}$

2

Q28 In how many ways can the letters of the word 'PERMUTATIONS' be arranged such that :

- a) P comes before S.
- b) Word start with P and end with S.
- c) All vowels are together
- d) P comes before S and there are always 4 letters between P and S.

Q29 a) A solution of 8% boric acid is to be diluted by adding a 2% boric acid solution to it. The resulting mixture is to be more than 4%, but less than 6% boric acid. If we have 640 litres of 8% solution, how many litres of 2% solution will have to be added ?

4

b) An electrician can be paid under two schemes as given below :

2

Scheme I : ₹ 500 and ₹ 70 per hour.

Scheme II : ₹ 120 per hour.

If the job takes 'x' hours, for what value of 'x' does the scheme I give the electrician better wages ?