

Exercise 5.1

1. Which of the following statements are true and which are false? Give reasons for your answers.

- (i) Only one line can pass through a single point.
- (ii) There are an infinite number of lines which pass through two distinct points.
- (iii) A terminated line can be produced indefinitely on both the sides.
- (iv) If two circles are equal, then their radii are equal.
- (v) In Fig. 5.9, if  $AB = PQ$  and  $PQ = XY$ , then  $AB = XY$ .



Fig. 5.9

Solution:

- (i) False  
There can be infinite number of lines that can be drawn through a single point. Hence, the statement mentioned is False
- (ii) False  
Through two distinct points there can be only one line that can be drawn. Hence, the statement mentioned is False
- (iii) True  
A line that is terminated can be indefinitely produced on both sides as a line can be extended on both its sides infinitely. Hence, the statement mentioned is True.
- (iv) True  
The radii of two circles are equal when the two circles are equal. The circumference and the centre of both the circles coincide; and thus, the radius of the two circles should be equal. Hence, the statement mentioned is True.
- (v) True  
According to Euclid's 1<sup>st</sup> axiom- "Things which are equal to the same thing are also equal to one another". Hence, the statement mentioned is True.

2. Give a definition for each of the following terms. Are there other terms that need to be defined first? What are they, and how might you define them?

- (i) parallel lines
- (ii) perpendicular lines
- (iii) line segment
- (iv) radius of a circle
- (v) square

# NCERT Solution For Class 9 Maths Chapter 5- Introduction to Euclid's Geometry

## Solution:

Yes, there are other terms which need to be defined first, they are:

Plane: Flat surfaces in which geometric figures can be drawn are known as plane. A plane surface is a surface which lies evenly with the straight lines on itself.

Point: A dimensionless dot which is drawn on a plane surface is known as point. A point is that which has no part.

Line: A collection of points that has only length and no breadth is known as a line. And it can be extended on both directions. A line is breadth-less length.

- (i) Parallel lines - Parallel lines are those lines which never intersect each other and are always at a constant distance perpendicular to each other. Parallel lines can be two or more lines.
- (ii) Perpendicular lines - Perpendicular lines are those lines which intersect each other in a plane at right angles then the lines are said to be perpendicular to each other.
- (iii) Line Segment - When a line cannot be extended any further because of its two end points then the line is known as a line segment. A line segment has 2 end points.
- (iv) Radius of circle - A radius of a circle is the line from any point on the circumference of the circle to the center of the circle.
- (v) Square - A quadrilateral in which all the four sides are said to be equal and each of its internal angle is right angles is called square.

### 3. Consider two 'postulates' given below:

- (i) Given any two distinct points A and B, there exists a third point C which is in between A and B.
- (ii) There exist at least three points that are not on the same line.

Do these postulates contain any undefined terms? Are these postulates consistent? Do they follow from Euclid's postulates? Explain.

## Solution:

Yes, these postulates contain undefined terms. Undefined terms in the postulates are:

- There are many points that lie in a plane. But, in the postulates given here, the position of the point C is not given, as of whether it lies on the line segment joining AB or not.

- On top of that, there is no information about whether the points are in same plane or not.

And

Yes, these postulates are consistent when we deal with these two situations:

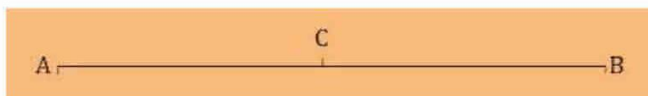
- Point C is lying on the line segment AB in between A and B.

- Point C does not lie on the line segment AB.

No, they don't follow from Euclid's postulates. They follow the axioms.

### 4. If a point C lies between two points A and B such that $AC = BC$ , then prove that $AC = \frac{1}{2} AB$ . Explain by drawing the figure.

## Solution:



# NCERT Solution For Class 9 Maths Chapter 5- Introduction to Euclid's Geometry

Given that,  $AC = BC$

Now, adding  $AC$  both sides.

$$\text{L.H.S} + AC = \text{R.H.S} + AC$$

$$AC + AC = BC + AC$$

$$2AC = BC + AC$$

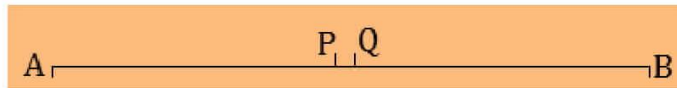
We know that,  $BC + AC = AB$  (as it coincides with line segment  $AB$ )

$$\therefore 2AC = AB \quad (\text{If equals are added to equals, the wholes are equal.})$$

$$\Rightarrow AC = (\frac{1}{2})AB.$$

**5. In Question 4, point  $C$  is called a mid-point of line segment  $AB$ . Prove that every line segment has one and only one mid-point.**

Solution:



Let,  $AB$  be the line segment

Assume that points  $P$  and  $Q$  are the two different mid points of  $AB$ .

Now,

$\therefore P$  and  $Q$  are midpoints of  $AB$ .

Therefore,

$$AP = PB \text{ and } AQ = QB.$$

also,

$$PB + AP = AB \text{ (as it coincides with line segment } AB)$$

Similarly,  $QB + AQ = AB$ .

Now,

Adding  $AP$  to the L.H.S and R.H.S of the equation  $AP = PB$

We get,  $AP + AP = PB + AP$  (If equals are added to equals, the wholes are equal.)

$$\Rightarrow 2AP = AB \text{ --- (i)}$$

Similarly,

$$2AQ = AB \text{ --- (ii)}$$

From (i) and (ii), Since R.H.S are same, we equate the L.H.S

$$2AP = 2AQ \text{ (Things which are equal to the same thing are equal to one another.)}$$

$$\Rightarrow AP = AQ \text{ (Things which are double of the same things are equal to one another.)}$$

Thus, we conclude that  $P$  and  $Q$  are the same points.

This contradicts our assumption that  $P$  and  $Q$  are two different mid points of  $AB$ .

Thus, it is proved that every line segment has one and only one mid-point.

Hence Proved.

**6. In Fig. 5.10, if  $AC = BD$ , then prove that  $AB = CD$ .**

Solution:



Fig. 5.10

It is given,  $AC = BD$

# NCERT Solution For Class 9 Maths Chapter 5- Introduction to Euclid's Geometry

From the given figure, we get,

$$AC = AB+BC$$

$$BD = BC+CD$$

$$\Rightarrow AB+BC = BC+CD \quad [AC = BD, \text{ given}]$$

We know that, according to Euclid's axiom, when equals are subtracted from equals, remainders are also equal.

$\therefore$ , Subtracting BC from the L.H.S and R.H.S of the equation  $AB+BC = BC+CD$ , we get,

$$AB+BC-BC = BC+CD-BC$$

$$AB = CD$$

Hence Proved.

**7. Why is Axiom 5, in the list of Euclid's axioms, considered a 'universal truth'? (Note that the question is not about the fifth postulate.)**

**Solution:**

Axiom 5: The whole is always greater than the part.

For Example: A cake. When it is whole or complete, assume that it measures 2 pounds but when a part from it is taken out and measured, its weigh will be smaller than the previous measurement.

So, the fifth axiom of Euclid is true for all the materials in the universe. Hence, Axiom 5, in the list of Euclid's axioms, is considered a 'universal truth'.

Exercise 5.2

**1. How would you rewrite Euclid's fifth postulate so that it would be easier to understand?**

**Solution:**

Euclid's fifth postulate: If a straight line falling on two straight lines makes the interior angles on the same side of it taken together less than two right angles, then the two straight lines, if produced indefinitely, meet on that side on which the sum of angles is less than two right angles.

i.e., the Euclid's fifth postulate is about parallel lines.

Parallel lines are the lines which do not intersect each other ever and are always at a constant perpendicular distance apart from each other. Parallel lines can be two or more lines.

A: If X does not lie on the line A then we can draw a line through X which will be parallel to that of the line A.

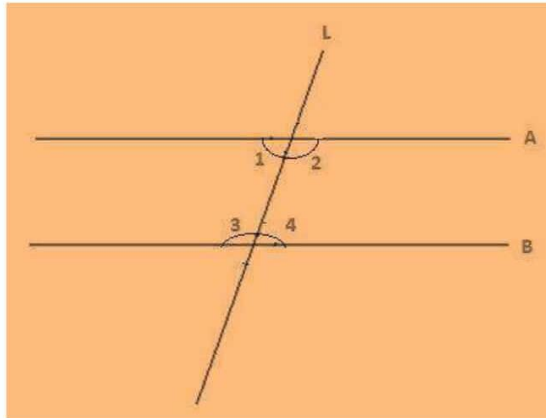
B: There can be only one line that can be drawn through the point X which is parallel to the line A.

**2. Does Euclid's fifth postulate imply the existence of parallel lines? Explain.**

**Solution:**

Yes, Euclid's fifth postulate does imply the existence of the parallel lines.

If the sum of the interior angles is equal to the sum of the right angles, then the two lines will not meet each other at any given point, hence making them parallel to each other.



Or  $\angle 1 + \angle 3 = 180^\circ$   
 $\angle 3 + \angle 4 = 180^\circ$