

EXERCISE 4.1

1. The linear equation $2x - 5y = 7$ has
 (a) a unique solution (b) two solutions
 (c) infinitely many solutions (d) no solution.

Sol. $2x - 5y = 7$ is a linear equation in two variables. A linear equation in two variables has infinitely many solutions.

Hence, (c) is the correct answer.

2. The equation $2x + 5y = 7$ has a unique solution if x, y are:
 (a) natural numbers (b) positive real numbers
 (c) real numbers (d) rational numbers.

Sol. The equation $2x + 5y = 7$ has a unique solution if x, y are natural numbers. Hence, (a) is the correct answer.

3. If $(2, 0)$ is a solution of the linear equation $2x + 3y = k$, then the value of k is:
 (a) 4 (b) 6 (c) 5 (d) 2

Sol. Substituting $x = 2$ and $y = 0$ in the given equation $2x + 3y = k$, we get
 $2(2) + 3(0) = k \Rightarrow k = 4$

Therefore, the value of k is 4.

Hence, (a) is the correct answer.

4. Any solution of the linear equation $2x + 0y + 9 = 0$ in two variables is of the form:

(a) $\left(-\frac{9}{2}, m\right)$ (b) $\left(n, -\frac{9}{2}\right)$ (c) $\left(0, -\frac{9}{2}\right)$ (d) $(-9, 0)$

Sol. The given linear equation is $2x + 0y + 9 = 0 \Rightarrow 2x = -9$

$$\therefore x = -\frac{9}{2}$$

Since the coefficient of y is 0 in the given equation, the solution can be

given as $\left(-\frac{9}{2}, m\right)$.

Hence, (a) is the correct answer.

5. The graph of the linear equation $2x + 3y = 6$ cuts the y -axis at the point
(a) (2, 0) (b) (0, 3) (c) (3, 0) (d) (0, 2)

Sol. The graph of the linear equation $2x + 3y = 6$ cuts the y -axis at the point where x -coordinate is zero.

Putting $x = 0$ in $2x + 3y = 6$, we get

$$2(0) + 3y = 6 \Rightarrow 3y = 6 \Rightarrow y = 6 \div 3 = 2$$

So, (0, 2) is the required point.

Hence, (d) is the correct answer.

6. The equation $x = 7$ in two variables can be written as

(a) $1.x + 1.y = 7$ (b) $1.x + 0.y = 7$

(c) $0.x + 1.y = 7$ (d) $0.x + 0.y = 7$

Sol. The equation $x = 7$ in two variables can be expressed as $1.x + 0.y = 7$.

Hence, (b) is the correct answer.

7. Any point on the x -axis is of the form

(a) (x, y) (b) $(0, y)$ (c) $(x, 0)$ (d) (x, x)

Sol. Any point on the x -axis has its ordinate 0.

So, any point on the x -axis is of the form $(x, 0)$.

Hence, (c) is the correct answer.

8. Any point on the line $y = x$ is of the form

(a) (a, a) (b) $(0, a)$ (c) $(a, 0)$ (d) $(a, -a)$

Sol. Any point on the line $y = x$ will have x and y coordinates same.

So, any point on the line $y = x$ is of the form (a, a) .

Hence, (a) is the correct answer.

9. The equation of x -axis is of the form

(a) $x = 0$ (b) $y = 0$ (c) $x + y = 0$ (d) $x = y$

Sol. $y = 0$ is the equation of x -axis.

Hence, (b) is the correct answer.

10. The graph of $y = 6$ is a line

(a) parallel to x -axis at a distance 6 units from the origin

(b) parallel to y -axis at a distance 6 units from the origin

(c) making an intercept 6 on the x -axis.

(d) making an intercept 6 on both the axes.

Sol. The given equation $y = 6$ does not contain x . Its graph is a line parallel to x -axis.

So, the graph of $y = 6$ is a line parallel to x -axis at a distance 6 units from the origin.

Hence, (a) is correct answer.

11. $x = 5, y = 2$ is a solution of the linear equation

(a) $x + 2y = 7$ (b) $5x + 2y = 7$ (c) $x + y = 7$ (d) $5x + y = 7$

Sol. $x = 5, y = 2$ is a solution of the linear equation $x + y = 7$, as $5 + 2 = 7$.

Hence, (c) is the correct answer.

12. If a linear equation has solutions $(-2, 2), (0, 0)$ and $(2, -2)$, then it is of the form

(a) $y - x = 0$ (b) $x + y = 0$ (c) $-2x + y = 0$ (d) $-x + 2y = 0$

Sol. The points $(-2, 2)$ and $(2, -2)$ have x and y coordinates of opposite signs.

Also, any point on the graph of $x + y = 0$

i.e., $y = -x$ will have x and y coordinates of opposite signs. The point $(0, 0)$ also satisfies $x + y = 0$.

Hence, (b) is the correct answer.

13. The positive solutions of the equation $ax + by + c = 0$ always lie in the

(a) 1st quadrant (b) 2nd quadrant

(c) 3rd quadrant (d) 4th quadrant

Sol. Quadrant I consists of all points (x, y) for which the x and y are positive. So, the positive solution of the equation $ax + by + c = 0$ always lie in the 1st quadrant.

Hence, (a) is the correct answer.

14. The graph of the linear equation $2x + 3y = 6$ is a line which meets the x -axis at the point

(a) $(0, 2)$ (b) $(2, 0)$ (c) $(3, 0)$ (d) $(0, 3)$

Sol. The graph of the linear equation $2x + 3y = 6$ is a line which meets the x -axis at the point where $y = 0$.

Now, putting $y = 0$ in $2x + 3y = 6$, we get

$$2x + 3(0) = 6 \Rightarrow 2x = 6 \Rightarrow x = 6 \div 2 = 3$$

So, $(3, 0)$ is a point on the line $2x + 3y = 6$.

Hence, (c) is the correct answer.

15. The graph of the linear equation $y = x$ passes through the point

(a) $\left(\frac{3}{2}, \frac{-3}{2}\right)$ (b) $\left(0, \frac{3}{2}\right)$ (c) $(1, 1)$ (d) $\left(\frac{-1}{2}, \frac{1}{2}\right)$

Sol. We know that any point on the line $y = x$ will have x and y coordinates same.

So, the graph of the linear equation $y = x$ passes through the point $(1, 1)$.

Hence, (c) is the correct answer.

16. If we multiply or divide both sides of a linear equation with a non-zero number, then the solution of the linear equation:

(a) changes (b) remains the same

(c) changes in case of multiplication only

(d) changes in case of division only

Sol. If we multiply or divide both sides of a linear equation with a non-zero number, then the solution of the linear equation remains the same.

Hence, (b) is the correct answer.

17. How many linear equations in x and y can be satisfied by $x = 1$ and $y = 2$?

- (a) Only one (b) Two (c) Infinitely many (d) Three

Sol. There are infinitely many linear equations which are satisfied by $x = 1$ and $y = 2$.

For example, a linear equation $x + y = 3$ is satisfied by $x = 1$ and $y = 2$. Others are $y = 2x$, $y - x = 1$, $2y - x = 3$ etc.

Hence, (c) is the correct answer.

18. The point of the form (a, a) always lies on:

- (a) x -axis (b) y -axis
(c) on the line $y = x$ (d) on the line $x + y = 0$

Sol. The point of the form (a, a) have x and y coordinates same. So, the point of the form (a, a) always lies on the line $y = x$.

Hence, (c) is the correct answer.

19. The point of the form $(a, -a)$ always lie on the line

- (a) $x = a$ (b) $y = -a$ (c) $y = x$ (d) $x + y = 0$

Sol. The point of the form $(a, -a)$ have x and y coordinates of opposite signs.

So, the point of the form $(a, -a)$ always lie on the line $y = -x$, i.e., $x + y = 0$.

Hence, (d) is the correct answer.

EXERCISE 4.2

Write whether the following statements are true or false. Justify your answer.

1. The point $(0, 3)$ lies on the graph of the linear equation $3x + 4y = 12$.

Sol. Substituting $x = 0$ and $y = 3$ in the equation, we get

$$3(0) + 4(3) = 12 \Rightarrow 12 = 12, \text{ which is true.}$$

The point $(0, 3)$ satisfies the equation $3x + 4y = 12$.

Hence, the given statement is true.

2. The graph of the linear equation $x + 2y = 7$ passes through the point $(0, 7)$.

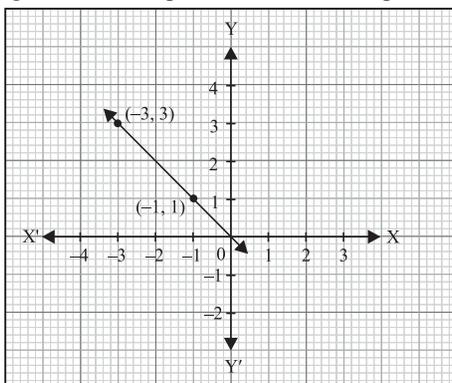
Sol. Substituting $x = 0$ and $y = 7$ in the given equation $x + 2y = 7$, we get

$$0 + 2(7) = 7 \Rightarrow 14 = 7, \text{ which is false.}$$

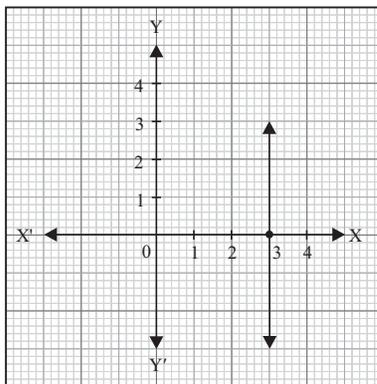
The point $(0, 7)$ does not satisfy the equation.

Hence, the given statement is false.

3. The graph given below represents the linear equation $x + y = 0$.



- Sol.** The given equation is $x + y = 0$, i.e., $y = -x$.
 Any point on the graph of $y = -x$, will have x and y coordinates of opposite signs.
 As the points $(-1, 1)$ and $(-3, 3)$ have x and y coordinates of opposite signs, so these points satisfy the given equation and the two points determine a unique line, hence the given statement is true.
4. The graph given below represents the linear equation $x = 3$. (See fig.)



- Sol.** We know that the graph of the equation $x = a$ is a line parallel to the y -axis and to the right of y -axis, if $a > 0$.
 The given statement is true, since the graph is a line parallel to y -axis at a distance of 3 units to the right of it.
5. The coordinates of points in the table:

x	0	1	2	3	4
y	2	3	4	-5	6

represent some of the solutions of the equation $x - y + 2 = 0$.

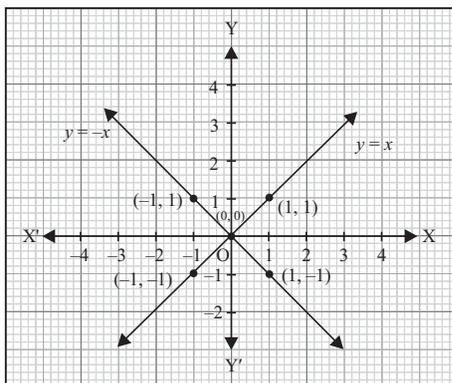
Sol. The points (0, 2), (1, 3), (2, 4) and (4, 6) satisfy the given equation $x - y + 2 = 0$. Each of these points is the solution of the equation $x - y + 2 = 0$. But, the point (3, -5) does not satisfy the given equation as $3 - (-5) + 2 = 0$, i.e., $3 + 5 + 2 = 0$ or $10 = 0$, which is false.

Hence, the given statement is false, since the point (3, -5) does not satisfy the given equation.

6. Every point on the graph of a linear equation in two variables does not represent a solution of the linear equation.
- Sol.** As every point on the graph of a linear equation in two variables represent a solution of the equation, so the given statement is false.
7. The graph of every linear equation in two variables need not be a line.
- Sol.** As the graph of a linear equation in two variables is always a line, so the given statement is false.

EXERCISE 4.3

1. Draw the graph of linear equations $y = x$ and $y = -x$ on the same cartesian plane. What do you observe?
- Sol.** Any point on the graph of $y = x$ will have x and y coordinates same. The line passes through the points $(0, 0)$, $(1, 1)$ and $(-1, -1)$.
 Again, any point on the graph of $y = -x$ will have x and y coordinates of opposite signs. The line passes through the points $(1, -1)$ and $(-1, 1)$. Also, $(0, 0)$ satisfies $y = -x$.
 The graph of linear equations $y = x$ and $y = -x$ on the same cartesian plane is shown in the figure given below.



- We observe that the graph of these equations passes through $(0, 0)$.
2. Determine the point on the graph of the linear equation $2x + 5y = 19$, whose ordinate is $1\frac{1}{2}$ times its abscissa.

Sol. Let the coordinates of the point be $(2, 3)$.

Now, for $x = 2$ and $y = 3$,

$$2x + 5y = 2(2) + 5(3) = 4 + 15 = 19$$

Therefore, the point $(2, 3)$ is a solution of the equation $2x + 5y = 19$.

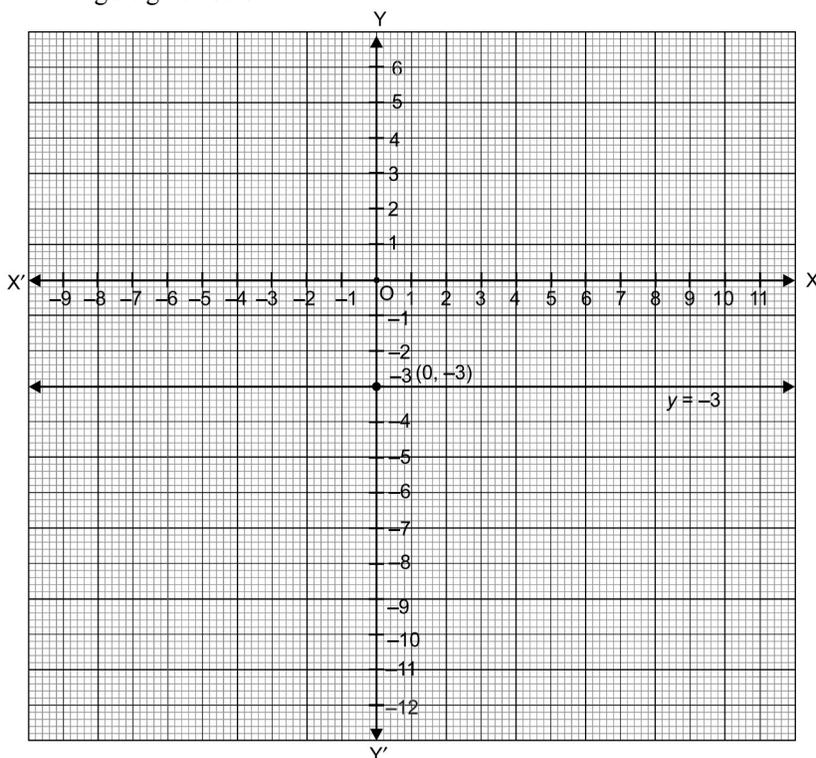
Abscissa of the point is 2 and ordinate is 3.

Now,
$$2 \times 1 \frac{1}{2} = 2 \times \frac{3}{2} = 3$$

So, ordinate of the point $(2, 3)$ is $1 \frac{1}{2}$ times its abscissa.

3. Draw the graph of the equation represented by a straight line which is parallel to the x -axis and at a distance 3 units below it.

Sol. The graph of the equation $y = -3$ is a line parallel to the x -axis and at a distance 3 units below it. So, graph of the equation $y = -3$ is a line parallel to x -axis and passing through the point $(0, -3)$ as shown in the figure given below:



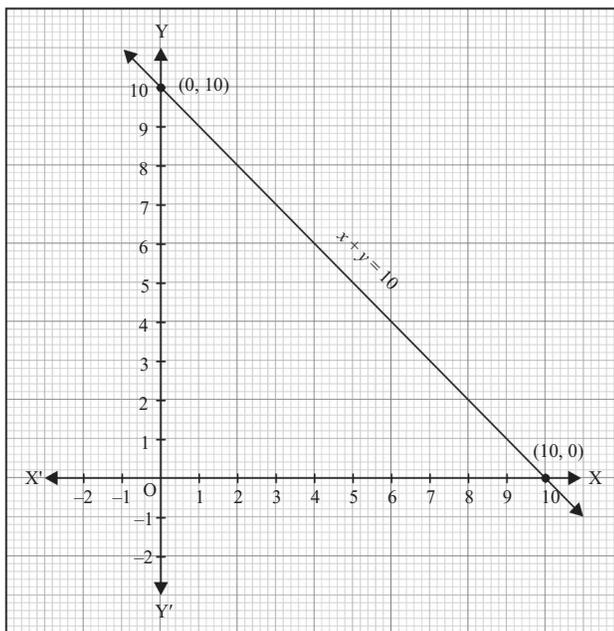
4. Draw the graph of the linear equation whose solutions are represented by the points having the sum of coordinates as 10 units.

Sol. A linear equation whose solutions are represented by the points having the sum of coordinates as 10 units is $x + y = 10$.

When $x = 0, y = 10$ and when $x = 10, y = 0$.

Now, plot these two points $(0, 10)$ and $(10, 0)$ on a graph paper and join them to obtain a straight line.

The graph of $x + y = 10$ is a straight line as shown in the figure given below.



5. Write the linear equation such that each point on its graph has an ordinate 3 times its abscissa.

Sol. A linear equation such that each point on its graph has an ordinate 3 times its abscissa is $y = 3x$.

6. If the point $(3, 4)$ lies on the graph of $3y = ax + 7$, then find the value of a .

Sol. The point $(3, 4)$ lies on the graph of $3y = ax + 7$.

Substituting $x = 3$ and $y = 4$ in the given equation $3y = ax + 7$, we get

$$\therefore 3 \times 4 = a \times 3 + 7$$

$$\Rightarrow 12 = 3a + 7 \Rightarrow 3a = 5 \Rightarrow a = \frac{5}{3}$$

7. How many solution(s) of the equation $2x + 1 = x - 3$ are there on the

(i) number line

(ii) Cartesian plane?

Sol. (i) The number of solution(s) of the equation $2x + 1 = x - 3$ which are on the number line is one.

$$2x + 1 = x - 3 \Rightarrow 2x - x = -3 - 1 \Rightarrow x = -4$$

$\therefore x = -4$ is the solution of the given equation.

(ii) The number of solution(s) of the equation $2x + 1 = x - 3$ which are on the cartesian plane are infinitely many solutions.

8. Find the solution of the linear equation $x + 2y = 8$ which represents a point on

(i) x -axis, (ii) y -axis.

Sol. We know that the point which lies on x -axis has its ordinate 0.

Putting $y = 0$ in the equation $x + 2y = 8$, we get

$$x + 2(0) = 8 \Rightarrow x = 8$$

A point which lies on y -axis has its abscissa 0.

Putting $x = 0$ in the equation $x + 2y = 8$, we get

$$0 + 2y = 8 \Rightarrow y = 4$$

9. For what value of c , the linear equation $2x + cy = 8$ has equal values of x and y for its solution?

Sol. The value of c for which the linear equation $2x + cy = 8$ has equal values of x and y

i.e., $x = y$ for its solution is

$$2x + cy = 8 \Rightarrow 2x + cx = 8 \quad [\because y = x]$$

$$\Rightarrow cx = 8 - 2x$$

$$\therefore c = \frac{8 - 2x}{x}, x \neq 0$$

10. Let y varies directly as x . If $y = 12$ when $x = 4$, then write a linear equation.

What is the value of y , when $x = 5$?

Sol. y varies directly as x .

$$\Rightarrow y \propto x,$$

$$\therefore y = kx$$

Substituting $y = 12$ when $x = 4$, we get

$$12 = k \times 4 \Rightarrow k = 12 \div 4 = 3$$

Hence, the required equation is $y = 3x$.

The value of y when $x = 5$ is $y = 3 \times 5 = 15$.

EXERCISE 4.4

1. Show that the points A(1, 2), B(-1, -16) and C(0, -7) lie on the graph of the linear equation $y = 9x - 7$.

Sol. For A(1, 2), we have $2 = 9(1) - 7 = 9 - 7 = 2$

For B(-1, -16), we have $-16 = 9(-1) - 7 = -9 - 7 = -16$

For C(0, -7), we have $-7 = 9(0) - 7 = 0 - 7 = -7$

We see that the line $y = 9x - 7$ is satisfied by the points $A(1, 2)$, $B(-1, -16)$ and $C(0, -7)$. Therefore, $A(1, 2)$, $B(-1, -16)$ and $C(0, -7)$ are solutions of the linear equation $y = 9x - 7$ and therefore, lie on the graph of the linear equation $y = 9x - 7$.

2. The following observed values of x and y are thought to satisfy a linear equation.

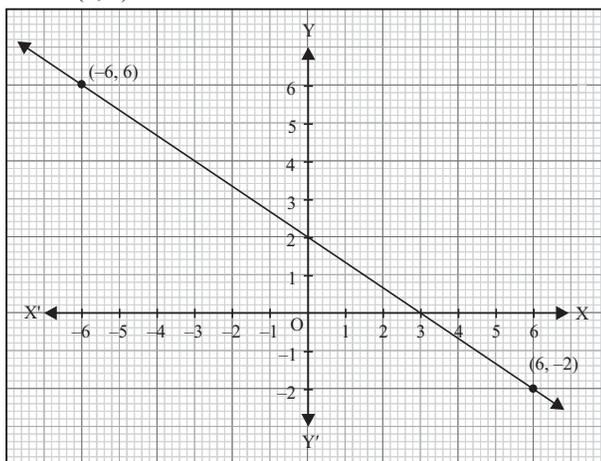
x	6	-6
y	-2	6

Write the linear equation.

Draw the graph using the values of x, y given in the above table. At what points, the graph of the linear equation cuts the x -axis and the y -axis?

- Sol.** The linear equation is $2x + 3y = 6$. Both the points $(6, -2)$ and $(-6, 6)$ satisfy the given linear equation.

Plot the points $(6, -2)$ and $(-6, 6)$ on a graph paper. Now, join these two points and obtain a line. We see that the graph cuts the x -axis at $(3, 0)$ and y -axis at $(0, 2)$.



3. Draw the graph of the linear equation $3x + 4y = 6$. At what points, the graph cuts the x -axis and y -axis?

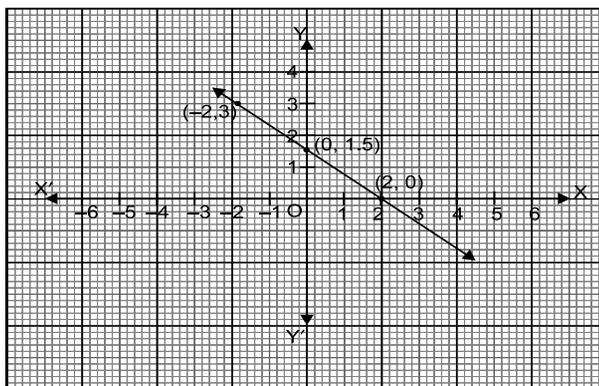
- Sol.** The solutions of the linear equation

$$3x + 4y = 6$$

can be expressed in the form of a table as follows by writing the values of y below the corresponding values of x :

x	2	-2	0
y	0	3	1.5

Now, plot the points $(2, 0)$, $(-2, 3)$ and $(0, 1.5)$ on a graph paper. Now, join the points and obtain a line.



We see that the graph cuts the x -axis at $(2, 0)$ and y -axis at $(0, 1.5)$.

4. The linear equation that converts Fahrenheit (F) to Celsius ($^{\circ}C$) is given by the relation:

$$C = \frac{5F - 160}{9}$$

- If the temperature is $86^{\circ}F$, what is the temperature in Celsius?
- If the temperature is $35^{\circ}C$, what is the temperature in Fahrenheit?
- If the temperature is $0^{\circ}C$, what is the temperature in Fahrenheit and if the temperature is $0^{\circ}F$, what is the temperature in Celsius?
- What is the numerical value of temperature which is same in both the scales?

Sol.

$$C = \frac{5F - 160}{9}$$

$$(i) \text{ Putting } F = 86^{\circ}, \text{ we get } C = \frac{5(86) - 160}{9} = \frac{430 - 160}{9} = \frac{270}{9} = 30^{\circ}$$

Hence, the temperature in celsius is $30^{\circ}C$.

$$(ii) \text{ Putting } C = 35^{\circ}, \text{ we get } 35^{\circ} = \frac{5F - 160}{9} \Rightarrow 315^{\circ} = 5F - 160$$

$$\Rightarrow 5F = 315 + 160 = 475$$

$$\therefore F = \frac{475}{5} = 95^{\circ}$$

Hence, the temperature in Fahrenheit is $95^{\circ}F$.

- (iii) Putting $C = 0^{\circ}$, we get

$$0 = \frac{5F - 160}{9} \Rightarrow 0 = 5F - 160$$

$$\Rightarrow 5F = 160$$

$$\therefore F = \frac{160}{5} = 32^{\circ}$$

Now, putting $F = 0^\circ$, we get

$$C = \frac{5F - 160}{9} \Rightarrow C = \frac{5(0) - 160}{9} = \left(-\frac{160}{9}\right)^\circ$$

If the temperature is 0° C, the temperature in Fahrenheit is 32° and if

the temperature is 0 F, then the temperature in Celsius is $\left(-\frac{160}{9}\right)^\circ$ C.

(iv) Putting $C = F$, in the given relation, we get

$$F = \frac{5F - 160}{9} \Rightarrow 9F = 5F - 160$$

$$\Rightarrow 4F = -160$$

$$\therefore F = \frac{-160}{4} = -40^\circ$$

Hence, the numerical value of the temperature which is same in both the scales is -40 .

The linear equation that converts Kelvin (x) to Fahrenheit (y) is given by the relation:

$$y = \frac{9}{5}(x - 273) + 32$$

5. If the temperature of a liquid can be measured in Kelvin units as x° K or in Fahrenheit units as y° F, the relation between the two systems of measurement of temperature is given by the linear equation

$$y = \frac{9}{5}(x - 273) + 32$$

(i) Find the temperature of the liquid in Fahrenheit if the temperature of the liquid is 313° K.

(ii) If the temperature is 158° F, then find the temperature in Kelvin.

Sol.
$$y = \frac{9}{5}(x - 273) + 32$$

(i) When the temperature of the liquid is $x = 313^\circ$ K

$$y = \frac{9}{5}(313 - 273) + 32 = \frac{9}{5} \times 40 + 32 = 72^\circ + 32^\circ = 104^\circ \text{ F}$$

(ii) When the temperature of the liquid is $y = 158^\circ$ F

$$158 = \frac{9}{5}(x - 273) + 32 \Rightarrow \frac{9}{5}(x - 273) = 158 - 32$$

$$\Rightarrow x - 273 = 126 \times \frac{5}{9} = 70$$

$$\Rightarrow x - 273 = 70 \Rightarrow x = 273 + 70 = 343^\circ \text{ K}$$

6. The force exerted to pull a cart is directly proportional to the acceleration produced in the body.

Express the statement as a linear equation in two variables and draw the graph of the same by taking the constant mass equal to 6 kg. Read from the graph, the force required when the acceleration produced in the body is
 (i) 5 m/s^2 (ii) 6 m/s^2 .

Sol. We have $y \propto x \Rightarrow y = m x$

where y denotes the force, x denotes the acceleration and m denotes the constant mass.

Taking $m = 6 \text{ kg}$, we get $y = 6x$.

Now, we form a table as follows by writing the values of y below the corresponding values of x .

x	0	1	2
y	0	6	12

Plot the points $(0, 0)$, $(1, 6)$ and $(2, 12)$ on a graph paper and join any two points and obtain a line.

